

LES FRACTIONS DE A À Z

EXERCICES RÉSOLUS

Exercice 1

SIMPLIFICATION ET CONVERSION DE FRACTIONS

On ne change pas un quotient quand on multiplie ou divise son numérateur et son dénominateur par un même nombre.

Simplifions sous forme irréductible les fractions :

$$\frac{6}{15} = \frac{6:3}{15:3} = \frac{2}{5}$$

$$\frac{12}{15} = \frac{12:3}{15:3} = \frac{4}{5}$$

$$\frac{20}{36} = \frac{20:4}{36:4} = \frac{5}{9}$$

$$\frac{72}{80} = \frac{72:8}{80:8} = \frac{9}{10}$$

$$\frac{30}{36} = \frac{30:6}{36:6} = \frac{5}{6}$$

$$\frac{12}{18} = \frac{12:6}{18:6} = \frac{2}{3}$$

$$\frac{35}{42} = \frac{35:7}{42:7} = \frac{5}{6}$$

$$\frac{120}{125} = \frac{120 \times 2}{125 \times 2} = \frac{240}{250} = \frac{24}{25}$$

$$\frac{11}{121} = \frac{11:11}{121:11} = \frac{1}{11}$$

$$\frac{13}{169} = \frac{13:13}{169:13} = \frac{1}{13}$$

Convertissons en pourcentages les fractions :

$$\frac{1}{2} = \frac{1 \times 50}{2 \times 50} = \frac{50}{100} = 50\%$$

$$\frac{1}{4} = \frac{1 \times 25}{4 \times 25} = \frac{25}{100} = 25\%$$

$$\frac{3}{4} = \frac{3 \times 25}{4 \times 25} = \frac{75}{100} = 75\%$$

$$\frac{3}{10} = \frac{3 \times 10}{10 \times 10} = \frac{30}{100} = 30\%$$

$$\frac{7}{10} = \frac{7 \times 10}{10 \times 10} = \frac{70}{100} = 70\%$$

$$\frac{1}{5} = \frac{1 \times 20}{5 \times 20} = \frac{20}{100} = 20\%$$

$$\frac{2}{5} = \frac{2 \times 20}{5 \times 20} = \frac{40}{100} = 40\%$$

$$\frac{3}{5} = \frac{3 \times 20}{5 \times 20} = \frac{60}{100} = 60\%$$

$$\frac{3}{20} = \frac{3 \times 5}{20 \times 5} = \frac{15}{100} = 15\%$$

$$\frac{9}{25} = \frac{9 \times 4}{25 \times 4} = \frac{36}{100} = 36\%$$

$$\frac{13}{20} = \frac{13 \times 5}{20 \times 5} = \frac{65}{100} = 65\%$$

$$\frac{17}{25} = \frac{17 \times 4}{25 \times 4} = \frac{68}{100} = 68\%$$

$$\frac{14}{50} = \frac{14 \times 2}{50 \times 2} = \frac{28}{100} = 28\%$$

$$\frac{41}{50} = \frac{41 \times 2}{50 \times 2} = \frac{82}{100} = 82\%$$

Exercice 2

COMPARAISON DE FRACTIONS

Comparons les fractions :

a) $\frac{3}{4}$ et $\frac{14}{20}$

b) $\frac{1}{3}$ et $\frac{5}{18}$

c) $\frac{1}{2}$ et $\frac{9}{20}$

d) $\frac{2}{3}$ et $\frac{5}{6}$

a) $\frac{3}{4} = \frac{3 \times 5}{4 \times 5} = \frac{15}{20} > \frac{14}{20}$

b) $\frac{1}{3} = \frac{1 \times 6}{3 \times 6} = \frac{6}{18} > \frac{5}{18}$

c) $\frac{1}{2} = \frac{1 \times 10}{2 \times 10} = \frac{10}{20} > \frac{9}{20}$

d) $\frac{2}{3} = \frac{2 \times 2}{3 \times 2} = \frac{4}{6} < \frac{5}{6}$

Exercice 3

PRODUIT D'UNE FRACTION PAR UN NOMBRE

Règle de calcul : $\frac{a}{b} \times c = \frac{a \times c}{b} = a \times \frac{c}{b}$
--

Réduisons sous forme irréductible :

$$\frac{7}{9} \times 9 = 7 \times \frac{9}{9} = 7 \times 1 = 7$$

$$\frac{9}{2} \times 2 = 9 \times \frac{2}{2} = 9 \times 1 = 9$$

$$\frac{3}{5} \times 10 = 3 \times \frac{10}{5} = 3 \times 2 = 6$$

$$\frac{3}{7} \times 14 = 3 \times \frac{14}{7} = 3 \times 2 = 6$$

$$\frac{3}{60} \times 24 = 3 \times \frac{24}{60} = 3 \times \frac{4}{10} = 3 \times \frac{2}{5} = \frac{6}{5}$$

$$45 \times \frac{1}{75} = \frac{45}{75} = \frac{9}{15} = \frac{3}{5}$$

$$\frac{32}{108} \times 3 = \frac{16}{54} \times 3 = \frac{8}{27} \times 3 = 8 \times \frac{3}{27} = 8 \times \frac{1}{9} = \frac{8}{9}$$

$$\frac{6}{7} \times 14 = 6 \times \frac{14}{7} = 6 \times 2 = 12$$

$$\frac{5}{9} \times 27 = 5 \times \frac{27}{9} = 5 \times 3 = 15$$

$$15 \times \frac{3}{10} = \frac{15}{10} \times 3 = \frac{3}{2} \times 3 = \frac{9}{2}$$

$$\frac{45}{70} \times 7 = \frac{9}{14} \times 7 = 9 \times \frac{7}{14} = 9 \times \frac{1}{2} = \frac{9}{2}$$

$$\frac{2}{150} \times 15 = 2 \times \frac{15}{150} = 2 \times \frac{1}{10} = \frac{2}{10} = \frac{1}{5}$$

$$\frac{4}{75} \times 25 = 4 \times \frac{25}{75} = 4 \times \frac{1}{3} = \frac{4}{3}$$

$$\frac{25}{1000} \times 10 = \frac{25}{100} = \frac{1}{4}$$

$$\frac{5}{11} \times 121 = 5 \times \frac{121}{11} = 5 \times 11 = 55$$

$$\frac{5}{42} \times 14 = 5 \times \frac{14}{42} = 5 \times \frac{1}{3} = \frac{5}{3}$$

Exercice 4

PRODUIT DE DEUX FRACTIONS

Règle de calcul : $\frac{a}{b} \times \frac{c}{d} = \frac{a \times c}{b \times d}$
--

Réduisons sous forme irréductible :

$$\frac{3}{10} \times \frac{10}{7} = \frac{3}{7} \times \frac{10}{10} = \frac{3}{7}$$

$$\frac{2}{7} \times \frac{7}{3} = \frac{2}{3} \times \frac{7}{7} = \frac{2}{3}$$

$$\frac{5}{3} \times \frac{3}{2} = \frac{5}{2} \times \frac{3}{3} = \frac{5}{2}$$

$$\frac{3}{5} \times \frac{4}{3} = \frac{3}{3} \times \frac{4}{5} = \frac{4}{5}$$

$$\frac{3}{4} \times \frac{8}{5} = \frac{3}{5} \times \frac{8}{4} = \frac{3}{5} \times 2 = \frac{6}{5}$$

$$\frac{2}{3} \times \frac{6}{5} = \frac{2}{5} \times \frac{6}{3} = \frac{2}{5} \times 2 = \frac{4}{5}$$

$$\frac{4}{5} \times \frac{10}{3} = \frac{4}{3} \times \frac{10}{5} = \frac{4}{3} \times 2 = \frac{8}{3}$$

$$\frac{5}{8} \times \frac{2}{3} = \frac{5}{3} \times \frac{2}{8} = \frac{5}{3} \times \frac{1}{4} = \frac{5}{12}$$

$$\frac{6}{5} \times \frac{10}{12} = \frac{6}{12} \times \frac{10}{5} = \frac{1}{2} \times 2 = 1$$

$$\frac{10}{11} \times \frac{22}{5} = \frac{10}{5} \times \frac{22}{11} = 2 \times 2 = 4$$